Problem:

Investigate linear dependence for the following system of functions: e^x , e^{x+1} .

Solution:

$$y_1 = e^x$$
, $y_2 = e^{x+1}$.

Using the definition of linear dependence $\alpha_1 y_1 + \alpha_2 y_2 = 0$, $e^x(\alpha_1 + \alpha_2 e) = 0$, $\Rightarrow \alpha_1 + \alpha_2 e = 0 \Rightarrow \alpha_1 + \alpha_2 e = 0$

$$\Rightarrow \alpha_1 = -\alpha_2 e, \alpha_2 = 1 \Rightarrow \alpha_1 = -e \Rightarrow -e \cdot y_1 + 1 \cdot y_2 = 0 \Rightarrow$$
 the functions are linearly dependent.

Answer: linearly dependent.