

Problem:

Let \overline{xy} and \overline{yx} be two two-digit integers. Prove that their sum is a composite number.

Solution:

 $\overline{xy} + \overline{yx} = 10x + y + 10y + x = 11(x + y) \vdots 11$, and since according to the condition \overline{xy} and \overline{yx} are two-digit $\Rightarrow x, y \ge 1 \Rightarrow x + y \ge 2 \Rightarrow 11(x + y) \ne 11 \Rightarrow$ it is composite $\Rightarrow \overline{xy} + \overline{yx}$ is a composite number.