



Problem:

Convert the formula to Zhegalkin polynomial.

$$(x\overline{y}z) \mid (x \mid (y \mid z)).$$

Solution:

$$f(x, y, z) = (x\overline{y}z) \mid (x \mid (y \mid z))$$

For the Sheffer stroke we have:

$$x \mid y = \overline{xy} \Rightarrow f(x, y, z) = (x\overline{y}z) \mid (x \mid (y \mid z)) = (x\overline{y}z) \mid (x \mid \overline{yz}) = (x\overline{y}z) \mid (\overline{x \cdot \overline{yz}}) =$$

De Morgan's law $\overline{xy} = \overline{x} \vee \overline{y}$

$$\Rightarrow (x\overline{y}z) \mid (\overline{x \vee \overline{yz}}) = (x\overline{y}z) \mid (\overline{x} \vee yz) = \overline{x \cdot \overline{y}z \cdot (\overline{x} \vee yz)} = \boxed{x \cdot \overline{x} \Rightarrow}$$

$= \overline{x \cdot \overline{y}z \cdot \overline{x} \vee x \cdot \overline{y}z \cdot yz} = \overline{0 \vee 0} = \overline{0} = 1 \Rightarrow f(x, y, z) = 1$, this is the desired Zhegalkin polynomial of the function $f(x, y, z)$ (in this case the polynomial is a constant, i.e., only the free term is nonzero).