



Problem:

Solve for all values of the parameter.

$$3x + 9 < m^2 - mx.$$

Solution:

$$3x + 9 < m^2 - mx \Rightarrow 3x + mx + 9 - m^2 < 0, x(m + 3) + (3 - m)(3 + m) < 0 \Rightarrow (m + 3)(x + 3 - m) < 0$$

when $m = -3 \Rightarrow 0 < 0$ a contradiction \Rightarrow there are no solutions. When $m < -3 \Rightarrow m + 3 < 0 \Rightarrow$

$\Rightarrow x + 3 - m > 0 \Rightarrow x > m - 3 \Rightarrow$ the solution to the inequality will be $(m - 3; +\infty)$.

When $m > -3 \Rightarrow m + 3 > 0 \Rightarrow x < m - 3 \Rightarrow$ the solution to the inequality will be $(-\infty; m - 3)$.

Answer: $m < -3$, the solution is $(m - 3; +\infty)$, $m = -3$, no solutions, $m > -3$, the solution is $(-\infty; -3)$.